

Classical and Quantum Mechanics

QUANTUM SPACETIME

MIMICRY OF PATHS
AND BLACK HOLES

Marco Spaans

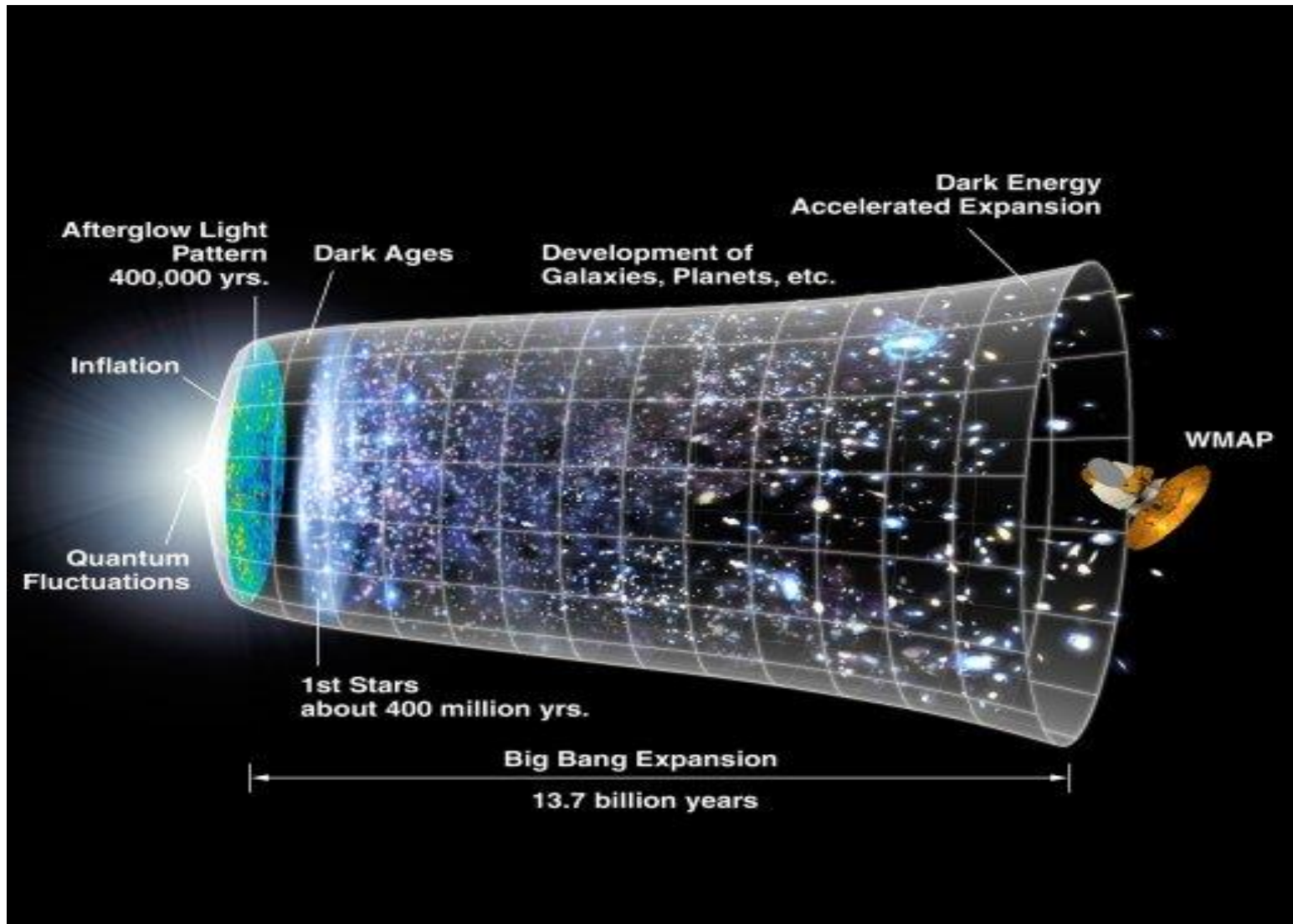
NOVA

Spacetime: Energy
Black Holes

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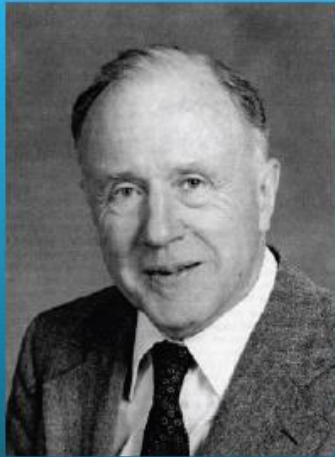
Cosmic evolution appears to involve inflation and dark energy



A Bit of General Relativity

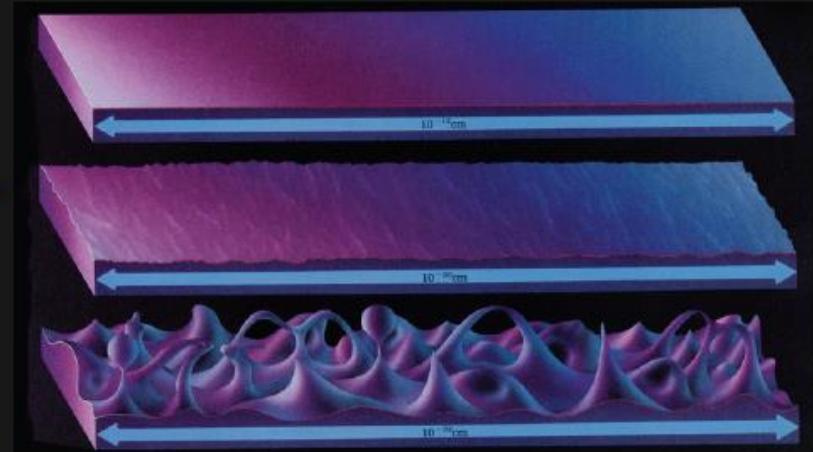
- Equivalence principle: Einstein's local interpretation of Mach's global principle.
- GR not invariant under local conformal transformations \rightarrow singular metric fluctuations on the Planck scale:
Wheeler's **quantum foam** of wormholes.
- The Einstein equation $G_{\mu\nu} = 8\pi G_N T_{\mu\nu}$ does not specify local and global **topology**.

Topology of Quantum Space-Time

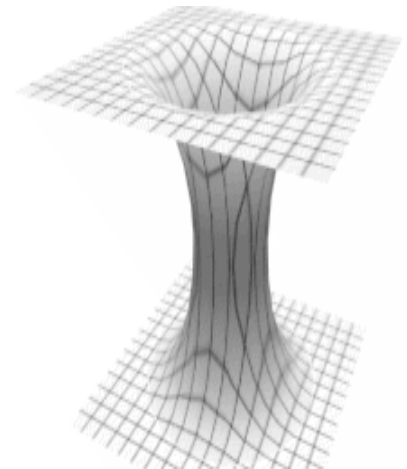


John Archibald Wheeler
1911-2008

Quantum Foam



On the **plank scale**, the universe
might be multiply connected:
wormholes (handles) $S^1 \times S^2$; m_p , l_p , t_p



Topology of Quantum Space-Time

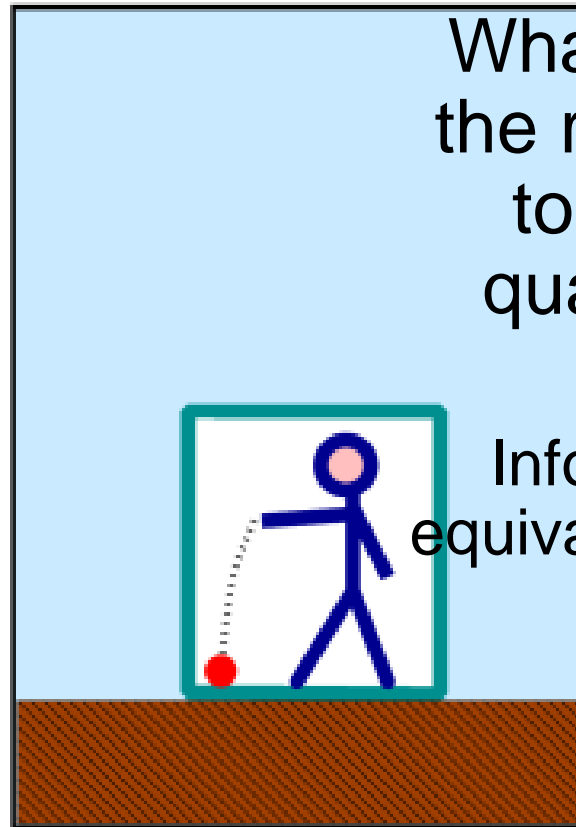
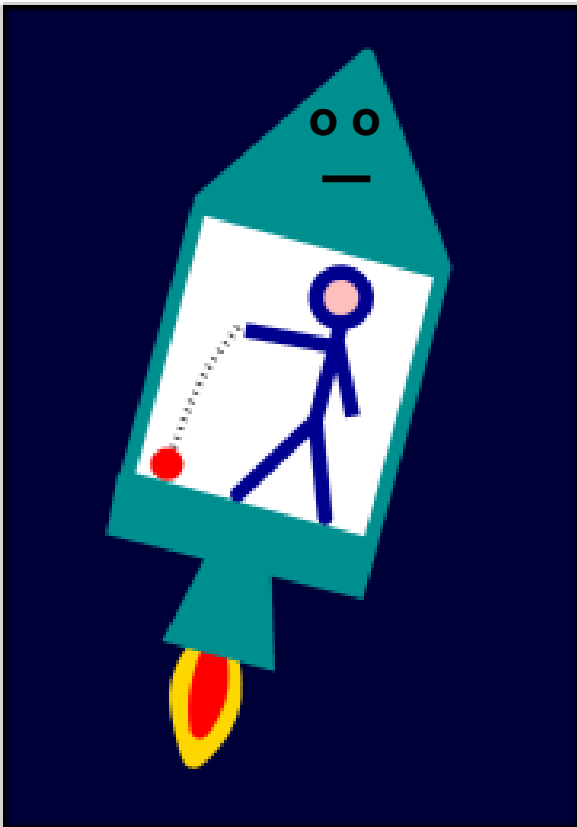


In topology, shapes or surfaces are considered to be equivalent if any continuous change can be continuously undone, this is called a homeomorphism.

A continuous deformation between a donut and a coffee cup.

This also means that there is no topological difference between a large and a small wormhole:
same information M , Q , S .

The Equivalence Principle: consider observer **and** observed



What **information** does the rocket operator need to **mimic** the proper quantum experience?

Information that is locally equivalent yet globally distinct.

Proposal:

Identity by Mimicry

- The collective existence of observers and observed derives from one **mimicking** the other unremittingly: They can adopt each other's role, so observers and observed are always **equivalent yet distinct**.
- No entity, like a particle or even a history, has individual significance; one needs a proper example to compare to.
- This mimicry also holds for black holes...
- Under the observational act of mimicry Wheeler's quantum foam of **mini wormholes** is then globally **induced by macroscopic black holes**.

Topological induction of mini BHs because of mimicry

- Every t_p a **pair** of mini wormholes is induced by a BH because it Hawking evaporates and thus behaves as a wormhole in a topological sense: the entrance and exit both require a BH mimic for their 4D (historical) identity.
- Planckian wormholes evaporate in about $t_{ev} \sim t_p$.
- **Macroscopic** BHs live longer than a Hubble time and generate globally **stable** quantum foam mass density Λ .
- $\Lambda = 2N_{BH} m_p / L_f^3$, with L_f the size of the universe when the first BH with $t_{ev} > t_{univ}$, forms: **L_f is frozen in** when a global 4-space topology in the sense of Mach emerges.
- In fact: $N_{BH} = Y_{star} \beta_{BH} (p_c L_f^3) / \mu_{BH}$ yields $p_c \sim 10^{14} \text{ g cm}^{-3}$ for $Y_{star} \sim 10^{-2}$, $\beta_{BH} \sim 10^{-3}$, $\mu_{BH} \sim 3M_o$, $N_{BH} \sim 10^{19}$ today
= a global density that matter experiences gravitationally
= a typical neutron star density...!

Dark Energy

- Cosmological observations suggest an accelerated expansion of the universe, usually attributed to some form of vacuum energy Λ : Einstein's cosmological constant in the form of dark energy (Riess ea 98, Perlmutter ea 98), with $\rho_0 \sim 10^{-29} \text{ g cm}^{-3}$.
- About $N_{\text{BH}} \sim 10^{19}$ today, in the observable universe.
- Topological induction yields dark energy that follows the **number** of macroscopic BHs in the universe.
Induced Planckian BHs require an increase in 4-volume for their embedding: $L_f \approx 2 \times 10^{14} \text{ cm}$ from ρ_0 and N_{BH} .
- Observed star/BH formation history of universe yields: $\Lambda(z)/\Lambda(0) \sim (1+z)^{-0.36}$, $z < 1$; a $\sim 30\%$ decline: $w \approx -1.1$, not constant, consistent with observations.
In fact, $w = -1.08 \pm 6\%$ (Hinshaw ea 13; Planck: Ade ea 15).

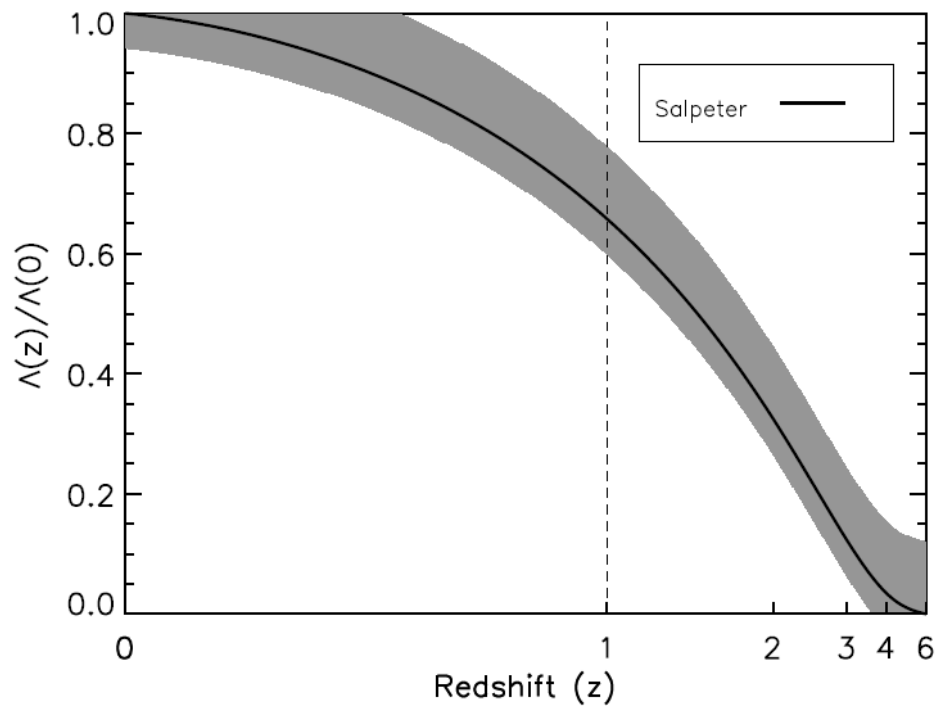


Fig. 1.— Redshift evolution of Λ derived from the type II SN rate data of Hopkins & Beacom (2006). The shading represents the observational uncertainty in deriving the type II SN rate.

Summary

- Observer-observed mimicry, implicit in Einstein's elevator thought experiment, expresses what equivalent yet distinct information is needed for gravity.
- This mimicry principle applied to black holes leads to the induction of Wheeler's quantum foam by the **number** of macroscopic BHs.

Thank You!

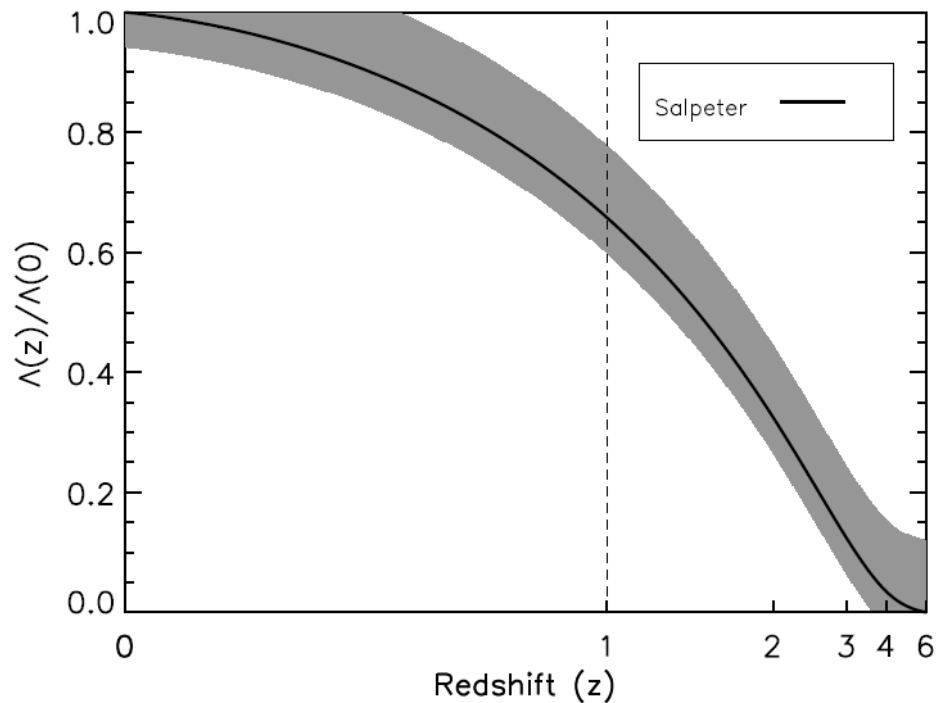
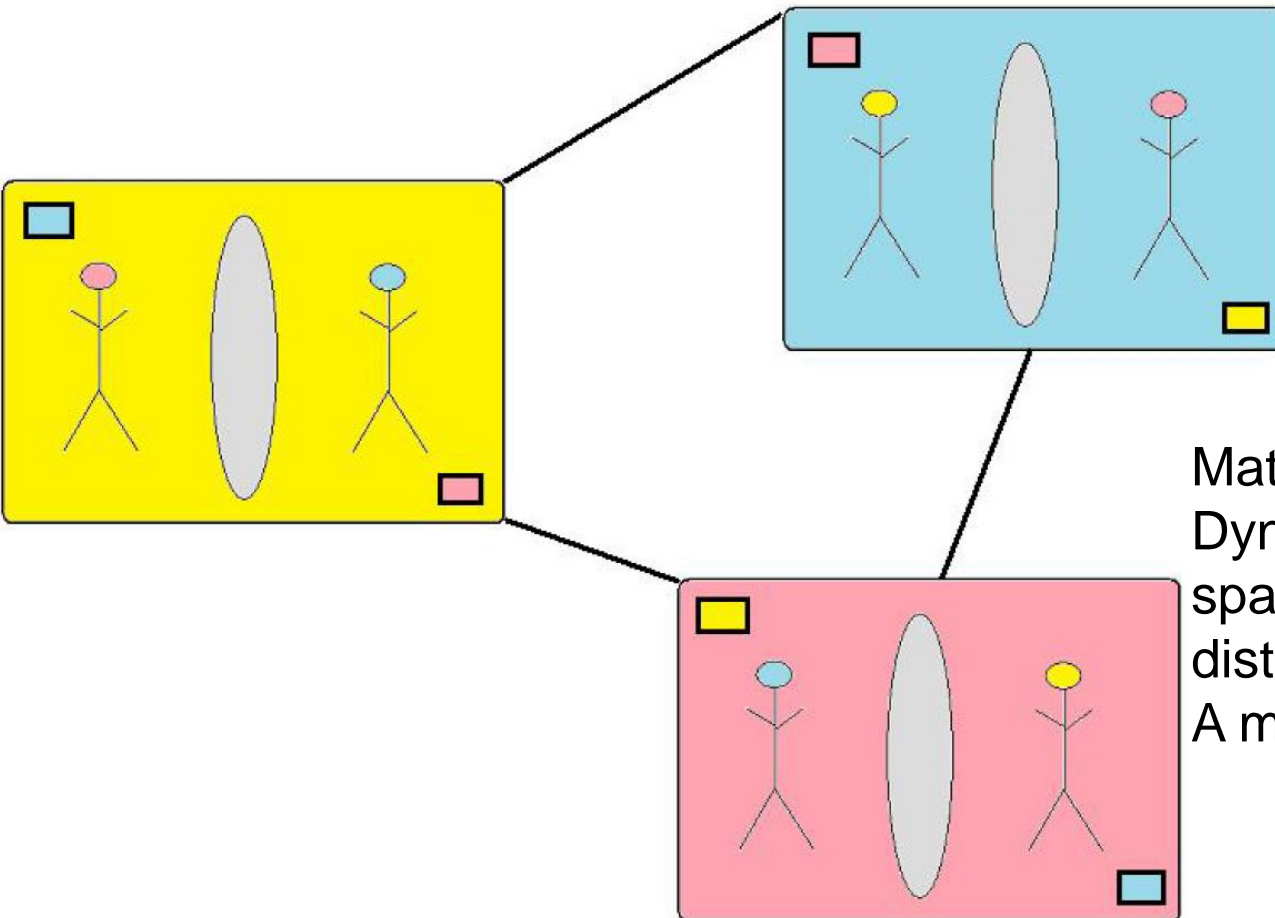


Fig. 1.— Redshift evolution of Λ derived from the type II SN rate data of Hopkins & Beacom (2006). The shading represents the observational uncertainty in deriving the type II SN rate.

The Mimicry Principle:

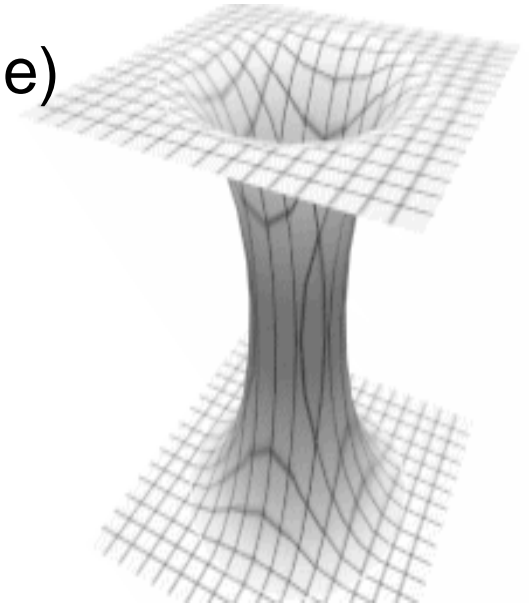
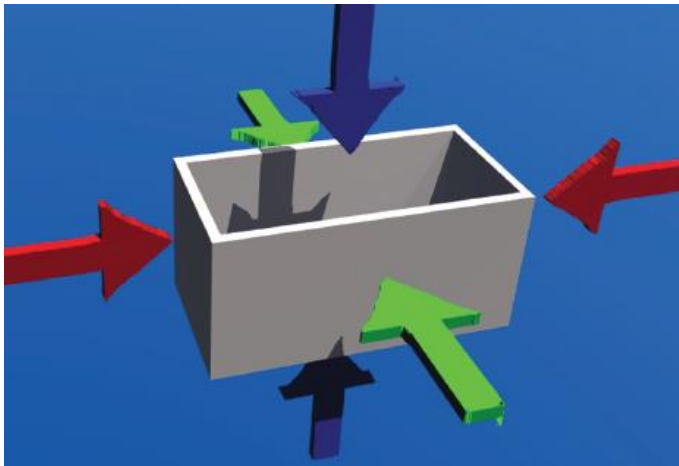
Any observer can mimic any observed's identity in terms of locally causal events, but only through the **induction** of four-space histories that are always globally distinct.



Matching colored squares =
Dynamical S^1 loops through 4-
space yield the induction of
distinct entangled histories =
A multiply connected universe

Multiply Connected Space-Time

- Topologically distinct paths, under **homeomorphisms**, between any two points:
- Use **loops** in T^3 , $S^1 \times S^2$ (and S^3 as glue)



- Build a **lattice** of three-tori, with spacing L_{Planck} , to travel through **4D** space-time as an expression of the superposition principle and attach Wheeler's handles: Quantum paths that connect points are then **globally identified** through **non-contractible** loops.

Such a lattice of three-tori yields Feynman's path integral

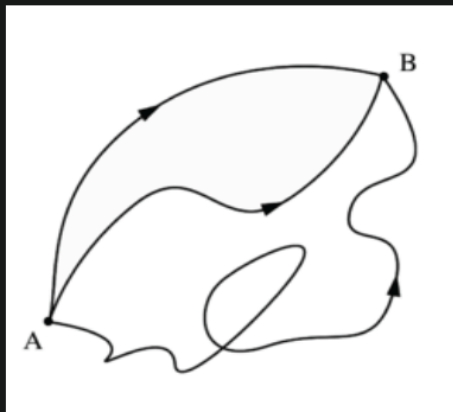
- A particle/wave travels along many paths as an expression of the **superposition principle**: connect any A to any B.
- $\int_{\text{paths}} e^{iS}$ leads to a semi-classical world line and a large scale limit for GR. But, how to distinguish paths on L_p ?

Topology of Quantum Space-Time

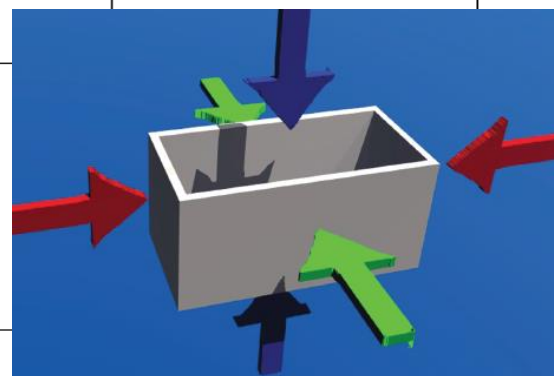
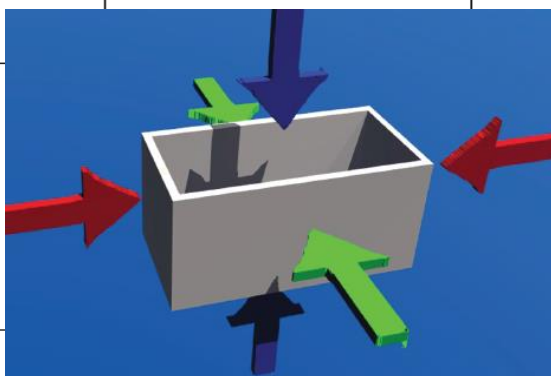
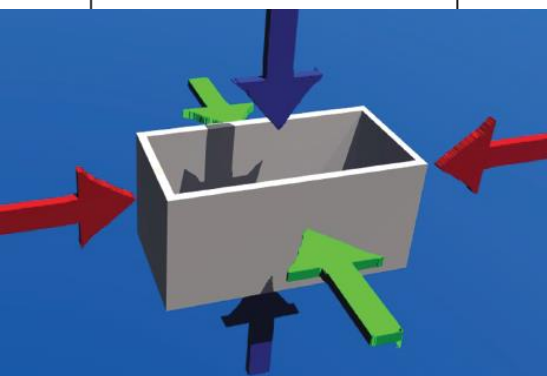
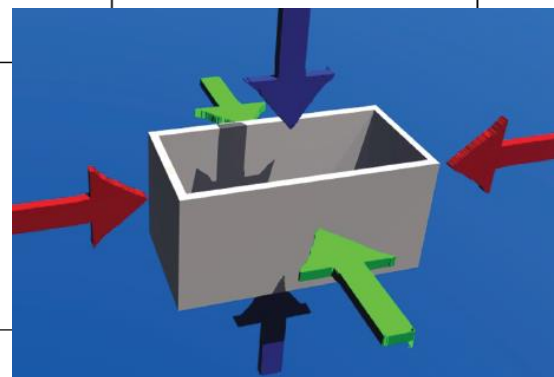
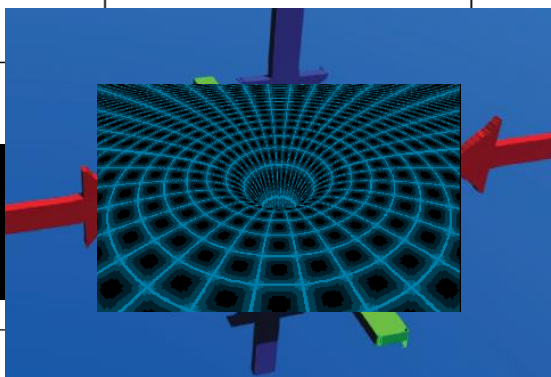
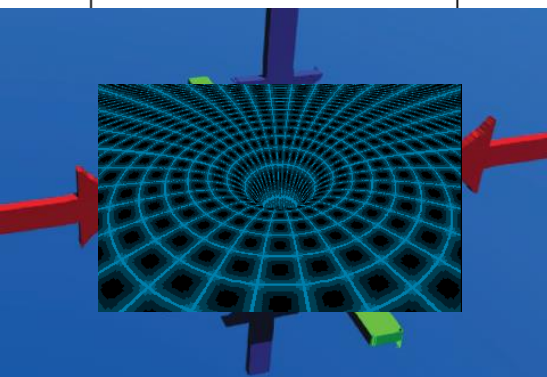
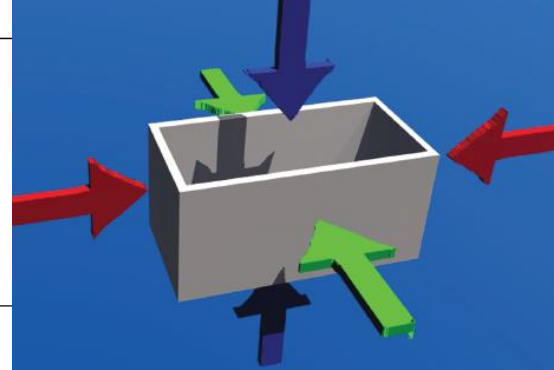
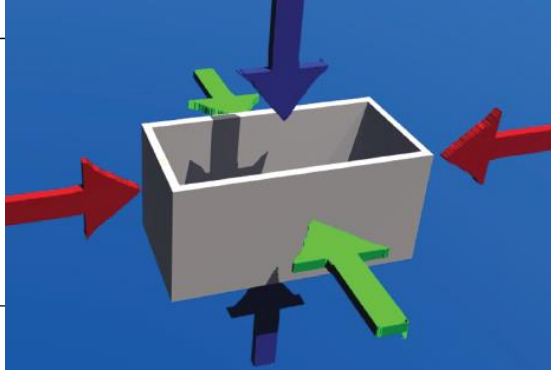
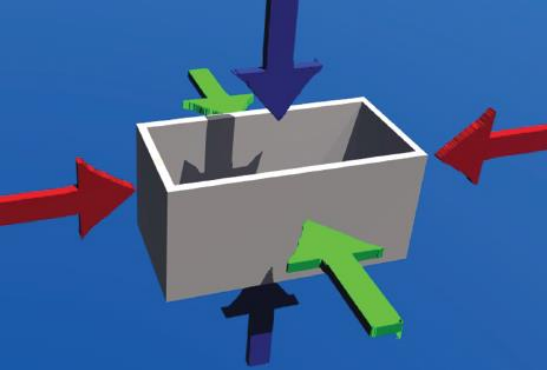


Richard Feynman
1918-1988

Path Integral



Observers cannot tell paths apart **locally**!



Summary

- Observer-observed mimicry, implicit in Einstein's elevator thought experiment, expresses what equivalent yet distinct information is needed for gravity.
- The mimicry principle applied to black holes leads to the induction of Wheeler's quantum foam by the **number** of macroscopic BHs, i.e., a testable form of dark energy.
- Inflation driven by induced mini BHs: $n \geq 55$ e-foldings, $n \sim \ln(L_f/L_{\text{Planck}})^{1/2} \sim \ln N_{\text{BH}}^{1/6}$.
- Further scrutiny of the lattice of three-tori leads to: quantum fluctuations with $n_s = 1 - r \approx \ln(7)/n = \mathbf{0.96}$.